Subject Code: YC Math 1



Subject: Matl

General Instructions:

Read the following instructions carefully and follow them:

- 1. This question paper contains 38 questions.
- 2. This Question Paper is divided into 5 Sections A, B, C, D and E.
- 3. In Section A, Questions no. 1-18 are multiple choice questions (MCQs) and questions no. 19 and 20 are Assertion- Reason based questions of 1 mark each.
- 4. In Section B, Questions no. 21-25 are very short answer (VSA) type questions, carrying 02 marks each.
- 5. In Section C, Questions no. 26-31 are short answer (SA) type questions, carrying 03 marks each.
- 6. In Section D, Questions no. 32-35 are long answer (LA) type questions, carrying 05 marks each.
- 7. In Section E, Questions no. 36-38 are case study based questions carrying 4 marks each with sub parts of the values of 1, 1 and 2 marks each respectively.
- 8. All Questions are compulsory. However, an internal choice in 2 Question of Section B, 2 Questions of Section C and 2 Questions of Section D has been provided. An internal choice has been provided in all the 2 marks questions of Section E.
- 9. Draw neat and clean figures wherever required.
- 10. Take $\pi = 22/7$ wherever required if not stated.
- 11. Use of calculators is not allowed.

	Section A					
	Section A consists of 20 questions of 1 mark each.					
1.	The graph of a quadratic polynomial $p(x)$ passes through the points (-6,0), (0, -30), (4,-20) and (6,0). The zeroes of the polynomial are	1				
	A) - 6,0 B) 4, 6 C) - 30,-20 D) - 6,6					
2.	The value of k for which the system of equations $3x-ky=7$ and $6x+10y=3$ is inconsistent, is	1				
	A) -10 B) -5 C) 5D) 7					
3.	Which of the following statements is not true?	1				
	A) A number of secants can be drawn at any point on the circle.					
	B) Only one tangent can be drawn at any point on a circle.					
	C) A chord is a line segment joining two points on the circle					
	D) From a point inside a circle only two tangents can be drawn.					

4.	If nth term of a	n A.P. is 7n-4 then th	e common difference of	the A.P. is	1
	A) 7	B) 7n	C) - 4	D) 4	

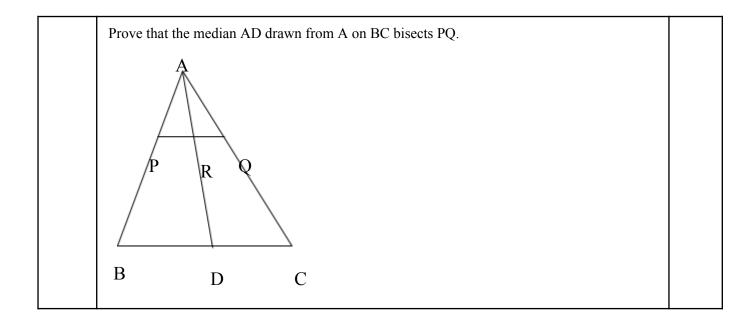
5.	The radius of the length. If the volucone is	_			-		1
	A) 5 cm	B) 20 cm	1	C) 10 cm	D) 4	4 cm	
6.	If $\tan \theta = -$ then 2	$\frac{4 \sin\theta + \cos\theta}{4 \sin\theta - \cos\theta}$ B) $\frac{3}{2}$	— is equal to	_ c) $\frac{c}{1}$	<u>)</u> 1	D) 4	1
7.	In the given figure	e, a tangent has	been drawn at	a point P on the	circle centred at	O.	1
	If \angle TPQ= 110° th A) 110°	en ∠POQ is equ	nal to B) 70 ⁰	C) 140	0	D)55 o	
8.	A) 110 B) 70 C) 140 D) 33 A quadratic polynomial having zeroes $-\sqrt{\frac{5}{2}}$ and $\sqrt{\frac{5}{2}}$ is A) $x^2 - 5\sqrt{2}x + 1$ B) $8x^2 - 20$ C) $15x^2 - 6$ D) $x^2 - 2\sqrt{5}x - 1$						
9.	Consider the frequency distribution of 45 observations.						1
	Class	0-10	10-20	20-30	30-40	40-50	
	Frequency	5	9	15	10	6	
	The upper limit o	f median class i	S				

	A) 20	B) 10	C) 30	D) 40	
10.	O is the point of intersecti	on of two chords AB an	d CD of a circle.		1
	D O O O A If $\angle BOC = 80^o$ and $OA = A$) equilateral and similar	C OD then ΔΟDA and ΔΟ	OBC are B) isosceles and	l similar	
	C) isosceles but not similar		D) not similar		
11.	The roots of the quadratic A) Irrational and distinct C) rational and distinct	equation $x^2 + x - 1 = 0$ are	B) not re D) real a		1
12.	If $\theta = 30^{\circ}$ then the value (A) 1 B) $\frac{1}{1}$		D) Not	defined	1
13	The volume of a solid her	39 misphere is —— <i>cm</i>	6 ³ .The total surface	e area of the solid	1
	hemisphere (in sq.cm) is	7			
	A) $\frac{396}{7}$ B) $\frac{59}{7}$	$\frac{4}{7}$ C) $\frac{54}{7}$	9	D) $\frac{604}{7}$	
14.	In a bag containing 24 bal random. The probability t			e white. One ball is drawn at	1
	A) 1 B)	_	-	D) ⁵	
15.	The point on the x- axis n	earest to the point (-4,-5)		8	1
	A) (0, 0) B)	(-4, 0) C) (-5, 0)	D) $(\sqrt{41}, 0)$	
16.	Which of the following gi A) Median B)		servation of the da C) Range	ta? D) Mode	1
17.	A point on the x-axis divide ratio 1:2. The point is	les the line segment join 7 3	ning the points A(2, -3) and B(5, 6) in the	1
	A) (4, 0) B)		(3, 0)	D) (0,3)	

		2 2				
18.	A card is drawn card is	from a well shuffled	deck of playing cards. Th	ne probability of getting red face	1	
	A) ³ _	B) 1	C) 3	D) ³		
	13	2	52	26		
	DIRECTION: In the question number 19 and 20, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct option A) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A) B) Both assertion (A) and reason (R) are true and reason (R) is not the correct explanation of assertion (A) C) Assertion (A) is true but reason (R) is false. D)Assertion (A) is false but reason (R) is true.					
19.	` ′	CF of any two consol numbers are divisil	ecutive even natural numb ble by 2.	ers is always 2. Reason	1	
20.	` ′	the radius of sector er of the sector rema		s half and angle is doubled	1	

	Reason (R): The length of the arc subtending angle θ at the centre of a circle of radius r = $\frac{Hr\theta}{2}$	
	180	
	Section B	
	Section B consists of 5 questions of 2 marks each.	
21.	(A)Find the H.C.F and L.C.M of 480 and 720 using the Prime factorisation method. OR (A) The H.C.F of 85 and 238 is expressible in the form 85m -238. Find the value of m.	2
22.	(A) Two dice are rolled together bearing numbers 4, 6, 7, 9, 11, 12. Find the probability that the product of numbers obtained is an odd number	2
	OR	
	(B) How many positive three digit integers have the hundredths digit 8 and unit's digit 5? Find the probability of selecting one such number out of all three digit	
	numbers.	

23.	$\frac{2\sin^2 60^o - \tan^2 30^o}{\text{Evaluate:}}$	2
	$sec^2 45^o$	
24.	Find the point(s) on the x-axis which is at a distance of $\sqrt{41}$ units from the point (8, -5).	2
25.	Show that the points A(-5,6), B(3, 0) and C(9, 8) are the vertices of an isosceles triangle.	2
	Section C	
	Section C consists of 6 questions of 3 marks each.	
26.	(A) In \triangle ABC, D, E and F are midpoints of BC,CA and AB respectively. Prove that \triangle FBD \sim \triangle DEF and \triangle DEF \sim \triangle ABC	3
	F E	
	B D C	
	OR	
	(B) In ΔABC, P and Q are points on AB and AC respectively such that PQ is parallel to BC.	



27.	The sum of two numbers is 18 and the sum of their reciprocals is 9/40. Find the numbers.	3
28.	If α and β are zeroes of a polynomial $6x^2$ - $5x+1$ then form a quadratic polynomial whose zeroes are α^2 and β^2 .	3
29.	If $\cos\theta + \sin\theta = 1$, then prove that $\cos\theta - \sin\theta = \pm 1$	3
30.	(A) The minute hand of a wall clock is 18 cm long. Find the area of the face of the clock described by the minute hand in 35 minutes. OR	3
	(B) AB is a chord of a circle centred at O such that ∠AOB=60°. If OA = 14	
	cm then find the area of the minor segment. (take $\sqrt{3}$ =1.73)	
	A B	
31.	Prove that $\sqrt{3}$ is an irrational number.	3
	Section D	
	Section D consists of 4 questions of 5 marks each	
32.	(A) Solve the following system of linear equations graphically: $x+2y=3$, $2x-3y+8=0$	5
	OR (B) Places A and B are 180 km apart on a highway. One car starts from A and another from B at the same time. If the car travels in the same direction at	

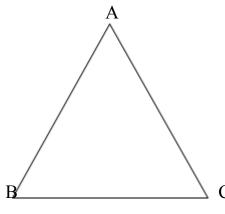
different speeds, they meet in 9 hours. If they travel towards each other with the same speeds as before, they meet in an hour. What are the speeds of the two cars?

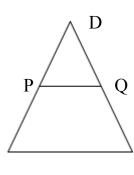
33.	Prove that	the lengt	hs of tan	gents draw	n from an	exte	rnal point	to a	circle	e are equ	al.	5
	∆ABC tou	Using above result, find the length BC of \triangle ABC. Given that, a circle is inscribed in \triangle ABC touching the sides AB, BC and CA at R, P and Q respectively and AB= 10 cm, AQ= 7cm, CQ= 5cm.										
	R Q B P C											
34.	horizontal eyes of the	-								5		
				$se \sqrt{3} = 1.7$								
35.	Find the n	Find the mean and median Class 85-90		of the follow 90-95	95-100		100-103	5	105	5-110	110-115	5
	frequency	15	2	22	20		18 20		20		25]
	The montl	nly expen	diture on	milk in 20	OR 00 families	of a	Housing	Socie	ety is	given be	elow	
	Monthly	1000-	1500-	2000-	2500-		000-	350		4000-	4500-	
	Expendit ure (in Rs.)	1500	2000	2500	3000	35	500	400	00	4500	5000	
	Number of families	24	40	33	х	30)	22		16	7	
		Find the value of x and also find the mean expenditure										
					Se	ectio	n E					
	Secti	ion E co	onsists	of 3 cas	se study	bas	ed que	stio	ns o	of 4 mai	rks each.	

36. Ms. Sheela visited a store near her house and found that the glass jars are arranged one above the other in a specific pattern. On the top layer there are 3 jars. In the next layer there are 6 jars. In the 3rd layer from the top there are 9 jars and so on till the 8th layer. On the basis of the above situation answer the following questions. 1 Write an A.P whose terms represent the number of jars in different layers starting from top . Also, find the common difference. 1 (ii) Is it possible to arrange 34 jars in a layer if this pattern is continued? Justify your answer. (A) If there are 'n' number of rows in a layer then find the expression for finding the (iii) 2 total number of jars in terms of n. Hence find S_8 . (iii) (B) The shopkeeper added 3 jars in each layer. How many jars are there in the 5th layer 2 from the top?









E F

Triangle is a very popular shape used in interior designing. The picture given above shows a cabinet designed by a famous interior designer.

Here the largest triangle is represented by \triangle ABC and smallest one with shelf is represented by \triangle DEF. PQ is parallel to EF.

(i) Show that \triangle DPQ \sim \triangle DEF.

	PQ	1
	(ii) If DP= 50 cm and PE = 70 cm then find \longrightarrow .	1
	EF	
	(iii) (A) If 2AB = 5DE and \triangle ABC \sim \triangle DEF then show that $\frac{perimeter\ of\ \triangle ABC}{perimeter\ of\ \triangle DEF}$ is constant.	2
	OR	
	(iii) (B) If AM and DN are medians of triangles ABC and DEF respectively then prove that Δ ABM $\sim \Delta$ DEN.	2
38.		
	Metallic silos are used by farmers for storing grains. Farmer Girdhar has decided to	
	build a new metallic silo to store his harvested grains. It is in the shape of a cylinder	
	mounted by a cone.	
	Dimensions of the conical part of a silo is as follows:	
	Radius of base = 1.5 m	
	Height = 2 m	
	Dimensions of the cylindrical part of a silo is as follows:	
	Radius = 1.5 m	
	Height = 7 m	
	On the basis of the above information answer the following questions.	
	(i) Calculate the slant height of the conical part of one silo.	1
	(ii) Find the curved surface area of the conical part of one silo.	1
	(iii)(A) Find the cost of metal sheet used to make the curved cylindrical part of 1 silo at the rate of $\stackrel{?}{\sim}2000$ per m^2 .	2
	OR	
	(iii) (B) Find the total capacity of one silo to store grains.	2





Q.No.	Section A	Marks
1.	D) -6,6	1
2.	B) -5	1
3.	D) From a point inside a circle only two tangents can be drawn.	1
4.	A) 7	1
5.	B) 20 cm	1
6.	A) $\frac{11}{9}$	1
7.	C) 140°	1
8.	B) 8x ² - 20	1

9.	C) 30	1
10.	B) isosceles and similar	1
11.	A) Irrational and distinct	1
12.	C) $\frac{3}{\sqrt{3}}$	1
13.	B) $\frac{594}{7}$	1
14.	B) $\frac{3}{8}$	1
15.	B) (-4, 0)	1
16.	A) median	1
17.	C) (3,0)	1
18.	D) $\frac{3}{26}$	1
19.	B)	1
20.	D)	1

	Section B	
21. (A)	$480 = 2^5 \times 3 \times 5$ $720 = 2^4 \times 3^2 \times 5$	
	LCM $(480,720) = 2^5 \times 3^2 \times 5 = 1440$	1/2
	HCF (480, 720) = 24 x 3x 5 = 240	1/2
	OR	
(B)	85 = 5x17, 238 = 2x7x17 HCF(85, 238) = 17	1
	17 = 85xm -238 m = 3	1

22.(A)	Total number of possible outcomes = 6x6=36 For a product to be odd, both the numbers should be odd. Favourable outcomes are (7,7) (7,9) (7,11) (9,7) (9,9) (9, 11) (11,7) (11,9)	1/2		
	(11,11) no. of favourable outcomes = 9 P (product is odd) = $\frac{9}{36}$ Or $\frac{1}{4}$	1 1/2		
	OR			
(B)	Total number of three-digit numbers = 900.			
	Numbers with hundredth digit 8 & and unit's digit 5 are 805,815, 825,,895	1		
	Number of favourable outcomes = 10	1/2		
	P(selecting one such number) = $\frac{10}{900}$ or $\frac{1}{90}$			
<u>-</u>		 		
23.	$2 \left(\frac{\sqrt{3}}{2}\right)^2 - \left(\frac{1}{\sqrt{3}}\right)^2$	1 ½		
	$(\sqrt{2})^2$	1/		
- 1	= '	1/2		

Let the required point be
$$(x,0)$$

$$\sqrt{(8-x)^2 + 25} = \sqrt{41}$$

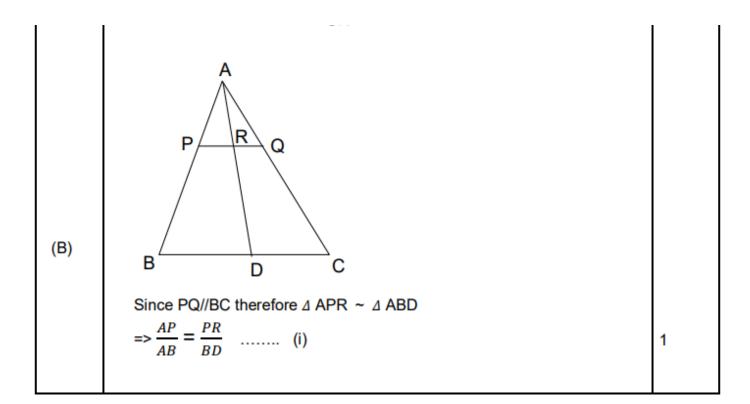
$$=> (8-x)^2 = 16$$

$$=> 8 - x = \pm 4$$

$$=> x = 4, 12$$
Two points on the x-axis are $(4,0)$ & $(12,0)$.

25.	$AB = \sqrt{(3+5)^2 + (0-6)^2} = 10$	1/2
	BC = $\sqrt{(9-3)^2 + (8-0)^2}$ = 10 AC = $\sqrt{(9+5)^2 + (8-6)^2}$ = $10\sqrt{2}$	1/2
	ΑΟ - γ (7 + 3) 1 (0 0) - 10 12	1/2
	Since AB = BC, therefore △ ABC is isosceles	1/2

	Section C	
26.(A)	Since D, E, F are the mid points of BC, CA, AB respectively Therefore, EF BC, DF AC, DE AB BDEF is a parallelogram $\angle 1 = \angle 2 \& \angle 3 = \angle 4$ $\triangle A = A = A = A = A = A = A = A = A = A $	1 1
	OR	



$$\Delta AQR \sim \Delta ACD$$

$$\Rightarrow \frac{AQ}{AC} = \frac{RQ}{DC} \qquad (ii)$$

$$Now, \frac{AP}{AB} = \frac{AQ}{AC} \qquad (iii)$$

$$Using (i), (ii) & (iii), \frac{PR}{BD} = \frac{RQ}{DC}$$

$$But, BD = DC$$

$$\Rightarrow PR = RQ \text{ or } AD \text{ bisects } PQ$$

28.	From given polynomial $\alpha + \beta = \frac{5}{6}$, $\alpha\beta = \frac{1}{6}$ $\alpha^2 + \beta^2 = (\frac{5}{6})^2 - 2 \times \frac{1}{6} = \frac{13}{36}$	1
	And $\alpha^2 \beta^2 = (\frac{1}{6})^2 = \frac{1}{36}$	1/2
	$x^2 - \frac{13}{36}x + \frac{1}{36}$ ⇒ Required polynomial is $36x^2 - 13x + 1$	1/2
29.	$(\cos\theta + \sin\theta)^2 + (\cos\theta - \sin\theta)^2 = 2(\cos^2\theta + \sin^2\theta) = 2$ => $(1)^2 + (\cos\theta - \sin\theta)^2 = 2$ => $(\cos\theta - \sin\theta)^2 = 1$ => $\cos\theta - \sin\theta = \pm 1$	1 ½ 1 ½

30.(A)	Angle described by minute hand in 5 min = 30°. length of minute hand =18 cm = r. Area swept by minute hand in 35 minutes $= (\frac{22}{7} \times 18 \times 18 \times \frac{30}{360}) \times 7$ $= 594 cm^2.$ OR	2
(B)	Area of minor segment = Ar. Sector OAB- Ar. \triangle OAB $= \frac{90}{360} \times \frac{22}{7} \times 14 \times 14 - \frac{\sqrt{3}}{4} \times 14 \times 14$ $= 69.23 \text{ cm}^2$	2

31.	Let $\sqrt{3}$ be a rational number. $\therefore \sqrt{3} = \frac{p}{q}$, where $q \neq 0$ and let p & q be co-prime. $3q^2 = p^2 \Rightarrow p^2$ is divisible by $3 \Rightarrow p$ is divisible by $3 \leftarrow \infty$ (i) $\Rightarrow p = 3a$, where 'a' is some integer $9a^2 = 3q^2 \Rightarrow q^2 = 3a^2 \Rightarrow q^2$ is divisible by $3 \Rightarrow q$ is divisible by $3 \leftarrow \infty$ (ii) (i) and (ii) leads to contradiction as 'p' and 'q' are co-prime.	1/ ₂ 1 1 1 1/ ₂	
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	Section D		
32.(A)	x+2y=3, 2x-3y+8=0 Correct graph of each equation Solution x=-1 and y=2	2+2 = 4 1	
	OR		
(B)	Let car I starts from A with speed x km/hr and car II Starts from B with speed y km/hr (x>y)		
	Case I- when cars are moving in the same direction. Distance covered by car I in 9 hours = 9x. Distance covered by car II in 9 hours = 9y Therefore 9 (x-y) = 180 => x-y= 20(i)	2	
	case II- when cars are moving in opposite directions.		
	Distance covered by Car I in 1 hour = x Distance covered by Car II in 1 hour = y		
	Therefore x + y=180(ii)	2	
	Solving (i) and (ii) we get, x=100 km/hr, y=80 km/hr.	1	

33.	Correct given, to prove, construction, figure	1
	Correct proof	2
	AR = AQ = 7cm BP = BR = AB-AR = 3cm CP = CQ = 5cm BC = BP+PC = 3+5 = 8 cm	1/2 1/2 1/2 1/2 1/2

34.	B "C	Correct figure 1mark
	h F 1.35 m	
	Let A be the eye level & B, C are positions of balloon Distance covered by balloon in 12 sec = 3x12 = 36 m BC = GF = 36 m	1
	tan $60^{0} = \sqrt{3} = \frac{h}{x}$ => h = $x \sqrt{3}$ (i)	1
	$\tan 30^{0} = \frac{1}{\sqrt{3}} = \frac{h}{x + 36}$ => h = $\frac{x + 36}{\sqrt{3}}$ (ii)	1
	Solving (i) and (ii) h= $18\sqrt{3}$ = 31.14 m Height of balloon from ground = 1.35 + 31.14 = 32.49 m	1

35.								Correct
		Class	x	f	$u = \frac{x - 102.5}{5}$	fu	cf	table 2marks
		85-90	87.5	15	-3	-45	15	
		90-95	92.5	22	-2	-44	37	
		95-100	97.5	20	-1	-20	57	
		100-105	102.5	18	0	0	75	
		105-110	107.5	20	1	20	95	
		110-115	112.5	25	2	50	120	
				Σf = 120		Σfu = -39		
	Me	dian class is	0.875	= 100.83				1 ½ ½ 1/2
					OR			

Monthly Expenditure	f_i	Xi	$f_i x_i$	Correct table
1000-1500	24	1250	30,000	2marks
1500-2000	40	1750	70,000	
2000-2500	33	2250	74,250	
2500-3000	X=28	2750	77,000	
3000-3500	30	3250	97,500	
3500-4000	22	3750	82,500	
4000-4500	16	4250	68,000	
4500-5000	7	4750	33,250	
172+x=200 X=28 Mean= $\frac{532500}{200}$				1
= 2662.5				1

	Section E	
36.(i)	First term a = 3, A.P is 3, 6, 9, 12,24 common difference d = 6-3 = 3	½ ½
(ii)	34 = 3 + (n-1)3 => $n = 34/3 = 11\frac{1}{3}$ which is not a positive integer.	1/2
	Therefore, it is not possible to have 34 jars in a layer if the given pattern is continued.	1/2
(iii)(A)	$S_n = \frac{n}{2} [2x3 + (n-1)3]$	1/2
	$= \frac{n^{2}}{2} [6 + 3n-3]$ $= \frac{n}{2} [3+3n]$ $= 3 \frac{n}{2} [1+n]$	1
	$s_8 = 3 \times \frac{8}{2} (1+8)$ = 108	1/2
	OR	
(iii) (B)	A.P will be 6, 9, 12, a= 6, d=3	1/2
	$t_5 = 6 + (5-1)3$ = 6 + 12	1
	= 18	1/2
		-
37. (i)	∠DPQ = ∠DEF	
	∠PDQ =∠EDF	1
(ii)	Therefore Δ DPQ ~ Δ DEF	1
	DE = 50 + 70 = 120 cm $\frac{DP}{DE} = \frac{PQ}{EF}$	1/2

	Therefore $\frac{PQ}{EF} = \frac{50}{120}$ or $\frac{5}{12}$	1/2
(iii) (A)	$\frac{AB}{DE} = \frac{5}{2} = \frac{BC}{EF} = \frac{AC}{DF}$ $\Rightarrow AB = \frac{5}{2}DE$	1
	$\frac{perimeter\ of\ \triangle ABC}{perimeter\ of\ \triangle DEF} = \frac{\frac{5}{2}(DE + EF + FD)}{DE + EF + FD} = \frac{5}{2} \text{ (Constant)}$	1
	OR	
(iii)(B)	AB BC BC/2 BM	Correct fig. ½ mark
	$\frac{AB}{DE} = \frac{BC}{EF} = \frac{BC/2}{EF/2} = \frac{BM}{EN}$ Also $\angle B = \angle E$	1
	Therefore \triangle ABM \sim \triangle DEN.	1/2

38. (i)	$ = \sqrt{r^2 + h^2} $ $= \sqrt{(1.5)^2 + (2)^2} $ $= \sqrt{2.25 + 4}$	1/2
	$=\sqrt{6.25}$ = 2.5 m	1/2
(ii)	CSA of cone = Π rl = $\frac{22}{5}$ x 1.5 x 2.5	1/2
	$= 11.78 m^2$	1/2
(iii) (A)	CSA of cylinder = 2π rh = $2 \times \frac{22}{7} \times 1.5 \times 7$	1
	= 66 m ² Cost of metal sheet used = 66 x 2000 = ₹1,32,000	1
(iii) (B)	OR Volume of cylinder = πr^2 h $= \frac{22}{7} \times (1.5)^2 \times 7$	
	$= 49.5 m^3$	1/2

Volume of cone = $\frac{1}{3} \Pi r^2 h$ = $\frac{1}{3} \times \frac{22}{7} \times (1.5)^2 \times 2$	
$= 4.71 m^3$	1
Total capacity = 49.5 + 4.71 = 54.21 m ³	1/2